MATIBIA UTIVERSITY
OF SCIEMCE AMD TECHMOLOGY

## FACULTY OF ENGINEERING AND THE BUILT ENVIRONMENT DEPARTMENT OF CIVIL MINING AND PROCESS ENGINEERING

| QUALIFICATION : BACHELORS OF ENGINEERING IN MINING ENGINEERING |  |
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| QUALIFICATION CODE: 08BMIN | LEVEL: 7 |
| COURSE CODE: REE720S | COURSE NAME: ROCK ENGINEERING |
| SESSION: NOVEMBER 2022 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SECOND OPPORTUNITY QUESTION PAPER |  |
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| EXAMINER(S) | Mallikarjun Rao Pillalamarry |
| MODERATOR: | Prof. Mapani Benjamin |

## INSTRUCTIONS

1. Answer all questions.
2. Read all the questions carefully before answering.
3. Marks for each question are indicated at the end of each question.
4. Please ensure that your writing is legible, neat and presentable.

PERMISSIBLE MATERIALS

1. Examination paper.
2. Tracing paper
3. Mathematical Instruments

THIS QUESTION PAPER CONSISTS OF 08 PAGES (Including this front page)

## Instructions: Answer Question 1 and any 4 other questions. Excess questions will not be marked.

Question 1 is compulsory.
Time allowed: 3 hours

## Question I

(20)

Short answer questions
a) What is pulp density of backfill? [1]
b) Why is the extraction ratio maintained at less than 0.75 in room and pillar mining? [1]
c) What are the conditions for wedge failure [2]
d) How are the crown holes (subsidence) formed? [1]
e) What is the optimum pulp density with respect to slurry back fill? [1]
f) What is the function of rib pillar? [1]
g) What factors influence the amount of subsidence tilt? [3]
h) Which rockmass parameters influence the stability of slopes? [2]
i) What are the different types of toppling failure? [3]
j) Which is the cheapest of backfills used in underground mines? [1]
k) What type of test is used to measure the bearing capacity of rockbolt? [1]

1) What is the point of inflexion with respect to subsidence? [1]
m) The sliding plane must 'daylight' in the slope face. What does this statement mean? [1]
n) Which one of these supports (rock bolts, steel sets and shotcrete) Figure 1 is stiffer?


Figure 1

## Question II

a) A 2 m radius vertical shaft is to be excavated through a sandstone in which in situ stresses are 4 and 6 MPa . A vertical discontinuity at its closest point A, located a distance of 6 m from shaft wall. The discontinuity has Coulomb shear strength parameters C is 0.05 MPa , angle of internal friction $(\phi)$ is $20^{\circ}$. Determine the factor of safety of discontinuity at point B shown in Figure 2.


Figure 2

## Question III

a) A metalliferous surface mine is operated with a bench as shown in Figure 3. The height of the bench is 10 m . The cohesion and angle of internal friction of failure plane are 15 kPa and $20^{\circ}$ respectively. Density of water and the rockmass is $1000 \mathrm{~kg} / \mathrm{m}^{3}$ and $3000 \mathrm{~kg} / \mathrm{m}^{3}\left(29.43 \mathrm{kN} / \mathrm{m}^{2}\right)$ respectively. Determine the effect water pressure in the crack on the factor of safety of the slope.


Figure 3
b) State the assumptions behind the derivation of Krisch equations used to determine stresses around underground openings.

## Question IV

a) Determine the subsidence tilt between the distance of $30-40 \mathrm{~m}$ from rib side under the following working conditions assuming that pre-subsidence profile is flat

- Depth of working 100 m
- Length of panel 150 m
- Mining height is 4 m
b) Briefly describe subsidence mechanism in high extraction mining


## Question V

a) A tunnel of 3 m radius excavated in a rock is subjected to a hydrostatic stress field of 10 MPa . Modulus of elasticity and Poisson's ratio of rockmass was estimated to be 600 MPa and 0.25 respectively. Assuming cohesion and angle of internal friction of rockmass is 2.42 MPa and $30^{\circ}$
i. Estimate longitudinal deformation 2 m away from the tunnel face
ii. Determine the factor of safety of shotcrete applied on to the surface of the tunnel at 2 m away from tunnel face with following specifications


Figure 4: Tunnel support characteristics curve

## Question VI

a) What are the properties of backfill and how does pore pressure influences the stability of backfill?
b) Compare mechanical anchored bolts with grouted rock bolts

## Additional Information

## Stresses around circular openings

$$
\begin{gathered}
\sigma_{r r}=\frac{p_{0}}{2}\left\{(1+k)\left(1-\frac{a^{2}}{r^{2}}\right)-(1-k)\left(1-4 \frac{a^{2}}{r^{2}}+3 \frac{a^{4}}{r^{4}}\right) \cos 2 \theta\right\} \\
\sigma_{\theta \theta}=\frac{p_{0}}{2}\left\{(1+k)\left(1+\frac{a^{2}}{r^{2}}\right)+(1-k)\left(1+3 \frac{a^{4}}{r^{4}}\right) \cos 2 \theta\right\} \\
\tau_{r \theta}=\frac{p_{0}}{2}\left\{(1-k)\left(1+2 \frac{a^{2}}{r^{2}}-3 \frac{a^{4}}{r^{4}}\right) \sin 2 \theta\right\}
\end{gathered}
$$

Displacement around circular openings

$$
\begin{gathered}
u_{r}=\frac{p_{0} a^{2}}{4 G r}\left\{(1+k)-(1-k)\left(4(1-v)-\frac{a^{2}}{r^{2}}\right) \cos 2 \theta\right\} \\
u_{\theta}=\frac{p_{0} a^{2}}{4 G r}\left\{(1-k)\left(2(1-2 v)+\frac{a^{2}}{r^{2}}\right) \sin 2 \theta\right\}
\end{gathered}
$$

Stresses around circular openings with internal pressure

$$
\begin{gathered}
\sigma_{r r}=p_{i}+\frac{\left(p_{o}-p_{i}\right)}{2}\left\{\left(1+k^{\prime}\right)\left(1-\frac{a^{2}}{r^{2}}\right)-\left(1-k^{\prime}\right)\left(1-\frac{4 a^{2}}{r^{2}}+3 \frac{a^{4}}{r^{4}}\right) \cos 2 \theta\right\} \\
\sigma_{\theta \theta}=p_{i}+\frac{\left(p_{o}-p_{i}\right)}{2}\left\{\left(1+k^{\prime}\right)\left(1+\frac{a^{2}}{r^{2}}\right)+\left(1-k^{\prime}\right)\left(1+3 \frac{a^{4}}{r^{4}}\right) \cos 2 \theta\right\} \\
\tau_{r \theta}=\frac{\left(p_{o}-p_{i}\right)}{2}\left\{\left(1-k^{\prime}\right)\left(1+\frac{2 a^{2}}{r^{2}}-3 \frac{a^{4}}{r^{4}}\right) \sin 2 \theta\right\} \\
k^{\prime}=\frac{k p_{0}-p_{i}}{p_{0}-p_{i}}
\end{gathered}
$$

Stresses around circular openings at infinite distance

$$
\sigma_{\theta \theta}=p_{0}[1+k+2(1-k) \cos 2 \theta]
$$

## Stress transformation

$$
\begin{gathered}
\sigma_{n}=\frac{1}{2}\left(\sigma_{r r}+\sigma_{\theta \theta}\right)+\frac{1}{2}\left(\sigma_{r r}-\sigma_{\theta \theta}\right) \cos 2 \alpha+\tau_{r \theta} \sin 2 \alpha \\
\tau_{n}=\tau_{r \theta} \cos 2 \alpha-\frac{1}{2}\left(\sigma_{r r}-\sigma_{\theta \theta}\right) \sin 2 \alpha
\end{gathered}
$$

## Support System Characteristics

$$
\sigma_{c}=\frac{2 c \cos \phi}{1-\sin \emptyset} \quad k=\frac{1+\sin \phi}{1-\sin \varnothing}
$$

$$
p_{c r}=\frac{2 p_{0}-\sigma_{c}}{1+k}
$$

Inward elastic displacement

$$
u_{i e}=\frac{r_{0}(1+v)}{E}\left(p_{0}-p_{i}\right)
$$

Radius of plastic zone around the tunnel

$$
r_{p}=r_{0}\left[\frac{2\left(p_{0}(k-1)+\sigma_{c}\right)}{(1+k)\left((k-1) p_{i}+\sigma_{c}\right)}\right]^{\frac{1}{(k-1)}}
$$

Total inward displacement

$$
u_{i p}=\frac{r_{0}(1+v)}{E}\left[2(1-v)\left(p_{0}-p_{c r}\right)\left(\frac{r_{p}}{r_{0}}\right)^{2}-(1-2 v)\left(p_{0}-p_{i}\right)\right]
$$

Longitudinal displacement
Ratio of maximum plastic zone radius to tunnel radius

$$
\frac{r_{p}}{r_{0}}=\left[\frac{2\left(p_{0}(k-1)+\sigma_{c}\right)}{(1+k) \sigma_{c}}\right]^{\frac{1}{(k-1)}}
$$

Displacement at tunnel face

$$
u_{i f}=\left(\frac{u_{i m}}{3}\right) e^{-0.15\left(\frac{r_{p}}{r_{0}}\right)}
$$

Maximum displacement

$$
u_{i m}=\frac{r_{0}(1+v)}{E}\left[2(1-v)\left(p_{0}-p_{c r}\right)\left(\frac{r_{p}}{r_{0}}\right)^{2}-(1-2 v) p_{0}\right]
$$

The tunnel wall displacement ahead of the face $(x<0)$ is

$$
u_{i}=u_{i f} e^{x / r_{0}}
$$

The tunnel wall displacement behind the face $(x>0)$ is

$$
u_{i}=u_{i m}-\left(u_{i m}-u_{i f}\right) e^{\frac{\left(-3 x / r_{0}\right)}{\left(2 r_{p} / r_{0}\right)}}
$$

## Rock Support Interaction

The displacement of the tunnel at support yield is given by

$$
u_{i y}=u_{i o}+\frac{p_{s m a x}}{K_{s}}
$$

The factor of safety (FS) of the support

$$
F S=\frac{p_{s \max }}{p_{s e}}
$$

Steel Support
.

$$
p_{s s \max }=\frac{A_{s} \sigma_{y s}}{s_{l} r_{0}} ; K_{s s}=\frac{A_{s} E_{s}}{s_{l} r_{0}^{2}}
$$

Shotcrete support

$$
p_{s c m a x}=\frac{\sigma_{c c}}{2}\left[1-\frac{\left(r_{0}-t_{c}\right)^{2}}{r_{0}^{2}}\right] ; K_{s c}=\frac{E_{c}\left(r_{0}^{2}-\left(r_{0}-t_{c}\right)^{2}\right)}{2\left(1-v^{2}\right)\left(r_{0}-t_{c}\right) r_{0}^{2}}
$$

Rock bolts

$$
p_{s b \max }=\frac{T_{b f}}{s_{l} s_{c}} ; K_{s b}=\frac{E_{s} \pi d_{b}^{2}}{4 l s_{l} s_{c}}
$$

Pillar design
Average pillar stress

$$
\sigma_{p}=\frac{\sigma_{z z}\left(w_{0}+w_{p}\right)^{2}}{w_{p}^{2}}
$$

Bearing capacity of roof/floor with square pillar

$$
\begin{gathered}
q_{b}=\frac{1}{2} \gamma w_{p} N_{\gamma}+c N_{c} \\
N_{c}=\left(N_{q}-1\right) \cot \phi ; N_{\gamma}=1.5\left(N_{q}-1\right) \tan \phi ; N_{q}=e^{\pi \tan \phi} \tan ^{2}\left[\left(\frac{\pi}{4}\right)+\left(\frac{\phi}{2}\right)\right]
\end{gathered}
$$

Bearing capacity of roof/floor with rib pillar

$$
\begin{gathered}
q_{b}=\frac{1}{2} \gamma w_{p} N_{\gamma} S_{\gamma}+c \cot \phi N_{q} S_{q}-c \cot \phi \\
S_{\gamma}=1-0.4\left(\begin{array}{c}
w_{p} / l_{p}
\end{array}\right) ; S_{q}=1+\sin \phi\left(w_{p} / l_{p}\right)
\end{gathered}
$$

## Subsidence

Maximum subsidence

$$
s_{m}=0.39 h\left(\frac{W}{H}\right)^{0.32}
$$

Subsidence at a distance $x$ from the rib side

$$
S_{x}=0.5 S_{m}\left[\tanh \left(\frac{7 x}{W}-1.645\right)+1\right]
$$

## Slope Stability

Planar slope failure

$$
F o S=\frac{c \mathrm{~A}+w \cos \psi_{p} \tan \phi}{w \sin \psi_{p}}
$$

Slope with Tension Crack in upper slope surface (From equations)

$$
\begin{aligned}
& F o S=\frac{c A+\left(w \cdot \cos \psi_{p}-U-V \cdot \sin \psi_{p}\right) \tan \phi}{w \cdot \sin \psi_{p}+V \cdot \cos \psi_{p}} \\
& A=\frac{(H-z)}{\sin \psi_{p}} ; U=\frac{\frac{1}{2} \gamma_{W} z_{w}(H-z)}{\sin \psi_{p}} ; V=\frac{1}{2} \gamma_{W} z_{W}^{2}
\end{aligned}
$$

Weight of sliding block (Slope with Tension Crack in upper slope surface)

$$
W=\frac{1}{2} \gamma H^{2}\left\{\left(1-(z / H)^{2}\right) \cos \psi_{p}-\cos \psi_{f}\right\}
$$

Weight of sliding block (Slope with Tension Crack in a slope face)

$$
W=\frac{1}{2} \gamma H^{2}\left\{\left(1-(z / H)^{2}\right) \cos \psi_{p}\left(\cot \psi_{p} \cdot \tan \psi_{f}-1\right)\right\}
$$

Factor of safety of the slope in dimensionless form (from Figures)

$$
\begin{gathered}
\mathrm{F}=\frac{(2 c / \gamma H) \cdot P+\left(Q \cdot \cot \psi_{p}-R(P+S)\right) \tan \phi}{Q+R \cdot S \cot \psi_{p}} \\
P=\frac{(1-z / H)}{\sin \psi_{p}} ; R=\frac{\gamma_{W}}{\gamma} \cdot \frac{Z_{W}}{z} \cdot \frac{Z}{H} ; S=\frac{z_{W}}{z} \cdot \frac{Z}{H} \cdot \sin \psi_{p}
\end{gathered}
$$

Slope with Tension Crack in the upper slope surface

$$
Q=\left\{\left(1-(z / H)^{2}\right) \cos \psi_{p}-\cos \psi_{f}\right\} \sin \psi_{p}
$$

Slope with Tension Crack in the slope face

$$
Q=\left\{\left(1-(z / H)^{2}\right) \cos \psi_{p}\left(\cot \psi_{p} \cdot \tan \psi_{f}-1\right)\right\}
$$

